

1. Na podstawie kilku początkowych wyrazów ciągu ustalić jego wzór ogólny

1. $(a_n) = (1, 4, 7, 10, \dots)$ 2. $(a_n) = (8, -4\sqrt{2}, 4, -2\sqrt{2}, \dots)$ 3. $(a_n) = (0, 1, 0, -1, 0, 1, -1, \dots)$

2. Dla podanych ciągów napisać wzory określające wskazane wyrazy ciągów

1. $a_n = \sqrt[n]{n^2 + 1}$, a_{n+1} 2. $a_n = \frac{1}{(2n)!}$, a_{3n+2} 3. $a_n = 3^n + 3^{n+1} + \dots + 3^{2n}$, a_{n^2}

3. Zbadać ograniczoność ciągów

1. $a_n = \sqrt{n+3} - \sqrt{n+5}$ 2. $a_n = \frac{3n + \sin n^2}{4n - \cos n!}$ 3. $a_n = \frac{1}{n^2+1} + \frac{1}{n^2+2} + \dots + \frac{1}{n^2+n}$

4. Zbadać czy podane ciągi są monotoniczne od pewnego miejsca

1. $a_n = n^2 - 49n - 50$ 2. $a_n = \frac{n+2}{n+5}$ 3. $a_n = \frac{2^n+1}{3^n+1}$

5. Oblicz granice ciągów

1. $a_n = \frac{n^3 + 2n^2 + n + 5}{2n^3 + n^2 + 3n + 1}$ 2. $a_n = \frac{(n+2)(n^2 + 3n + 1)}{(3n^3 + 2n^2 + 5n + 1)}$ 3. $a_n = \frac{(n^2 + 5n + 1)^3(n+3)^4}{(n^2 + 3n + 1)^5}$
 4. $a_n = \frac{(2n^3 + n^2 + 1)^2(n^2 + 1)^3}{(n^3 + 3n + 1)^4}$ 5. $a_n = \frac{n^4 + 3n^2 + 4n + 1}{n^3 + 3n^2 + n + 1}$ 6. $a_n = \frac{(n^2 + 3n + 5)^3(n^2 + n + 5)}{(n+2)^2(n-1)}$
 7. $a_n = \frac{n^3 + 3n^2 + 5n + 1}{n^4 + 2n^3 + n + 5}$ 8. $a_n = \frac{(4n^2 + 2n + 2)^3}{(n^3 + 3n^2 + n + 4)^3}$ 9. $a_n = \frac{\sqrt{9n^2 + 3n + 1}}{n + 5}$
 10. $a_n = \frac{n^2 + 5n + 1}{\sqrt[3]{8n^6 + n^2 + 3}}$ 11. $a_n = \sqrt{\frac{3n^2 + n + 1}{n^2 + 5n + 1}}$ 12. $a_n = \frac{\sqrt{n^2 - 1}}{\sqrt[3]{n^3 + 1}}$
 13. $a_n = \frac{(n+2)! + (n+1)!}{(n+2)! - (n+1)!}$ 14. $a_n = \frac{\binom{n+2}{n}}{n^2}$ 15. $a_n = \frac{1}{n} \binom{n}{1} + \frac{2}{n^2} \binom{n}{2} + \frac{1}{n^3} \binom{n}{3}$
 16. $a_n = \frac{1 + 3 + 5 + \dots + (2n-1)}{2n^2 + 3n + 2}$ 17. $a_n = \frac{1 - 2 + 3 - \dots - 2n}{3n^2 + 4n + 5}$ 18. $a_n = \frac{1 + \frac{1}{2} + \frac{1}{4} + \dots + \frac{1}{2^n}}{\frac{1}{3} + \frac{1}{9} + \dots + \frac{1}{3^n}}$
 19. $a_n = \frac{2^n + 3^{n+2}}{4 \cdot 3^{n+1} + 2^{n-2}}$ 20. $a_n = \frac{5 \cdot 5^{2n+1} - 3 \cdot 4^{2n+1}}{25^{n+1} + 16^{n+3}}$ 21. $a_n = \frac{3 \cdot 2^{3n+2} + 4^{2n+1}}{3^{2n+1} + 5 \cdot 5^{n-3}}$

6. Oblicz granice ciągów

1. $a_n = (\sqrt{n^2 + 2n + 2} - \sqrt{n^2 + 3n + 1})$ 2. $a_n = (3n - \sqrt{9n^2 + 5n + 1})$ 3. $a_n = (2n - \sqrt{4n^2 + 4n + 6})$
 4. $a_n = (\sqrt[3]{n^3 + 2n^2} - \sqrt[3]{n^3 + 2n + 1})$ 5. $a_n = (\sqrt{2n^2 + 4n + 5} - \sqrt{2n})$ 6. $a_n = (\sqrt{2n^2 + 2} - \sqrt{n^2 + 3n})$

7. Oblicz granice ciągów

1. $a_n = \sqrt[n]{2 \cdot 3^n + 5 \cdot 7^n}$ 2. $a_n = \sqrt[n]{5n^2 + \cos n}$ 3. $a_n = \sqrt{\frac{(-1)^n}{n}} + 2n$
 4. $a_n = \frac{1}{n^2+1} + \frac{2}{n^2+2} + \dots + \frac{n}{n^2+n}$ 5. $a_n = n(\frac{1}{n^2+1} + \frac{1}{n^2+2} + \dots + \frac{1}{n^2+n})$ 6. $a_n = (-1)^{n+3} \frac{n+1}{n^2+2n+3}$
 7. $a_n = \frac{\sin(n! + 2)}{n^2 + 3n + 1}$ 8. $a_n = \frac{3n + \sin n}{4n - \cos(n^2 + 1)}$ 9. $a_n = \frac{[n] + 3n}{n^2 + 2n + 5}$

8. Oblicz granice ciągów

1. $a_n = \left(1 - \frac{1}{n}\right)^n$

2. $a_n = \left(\frac{3n+1}{3n-1}\right)^{n+3}$

3. $a_n = \left(\frac{2n+2}{2n+4}\right)^{3n+1}$

4. $a_n = \left(\frac{n^2+1}{n^2}\right)^{\binom{n}{2}}$

5. $a_n = \left(\frac{4n-2}{4n+1}\right)^{3n-1}$

6. $a_n = \left(\frac{n^2+3}{n^2+1}\right)^{2n^2+5}$

9. Oblicz granice ciągów

1. $a_n = \frac{\log_2 n^5}{\log_8 n}$

2. $a_n = \frac{9^{\log_3 n}}{4^{\log_2 n}}$

3. $a_n = \frac{8^{\log_2 n}}{2^n}$

4. $a_n = \frac{27^{\log_3 n}}{16^{\log_2 n}}$

5. $a_n = \frac{n!}{n^n}$

6. $a_n = \frac{2^n \cdot 3^{2n}}{n!}$

7. $a_n = \left(1 - \frac{1}{2^2}\right) \left(1 - \frac{1}{3^2}\right) \dots \left(1 - \frac{1}{n^2}\right)$